Mathematics for Economics  
ECON 627, Fall 2009  
MW 10:30-11:45AM  SAUNDERS 541

Instructor: Nori Tarui  
Office: Saunders 518  
Phone: 956-8427  
Email: nori@hawaii.edu  
Office Hours: MW 3:00PM-4:00PM and by appointment.

Teaching Assistant: TBA  
Office: TBA  
Office hours: TBA  
Email: TBA

Course Content and Objectives

• The goal of this course is to prepare you for, or remind you of, the mathematical underpinnings of economic theory courses–Econ 606, 607, 608 and 609. To that end, we will seek to translate undergraduate economic theory topics into the language of mathematics, taking considerable care to develop the necessary mathematical framework and adding a few bells and whistles in the process. In addition, several increasingly important topics in economic theory are inherently mathematical–notably dynamic optimization models that form the basis of macroeconomic growth theory, natural resources exploitation models and other “dynamic” topics. We will cover both the mathematics and economics of these subjects, though only briefly.

• Ideally, we would cover each topic in this course just in time for the theory courses to use that topic. Inevitably, we will miss the timing on at least some topics. If the theory courses arrive at some topic that requires mathematics we have not yet covered in this course, you will nonetheless be expected to read mathematical appendices or other textbooks for that course to obtain at least an intuitive feel for the mathematics. Of course, you are also welcome to request adjustments in our schedule, and I will try to accommodate.

Prerequisites

MATH 203, MATH 215, MATH 241, MATH 251A or equivalent. Familiarity with the topics covered in the summer math cram course (offered by the Department of Economics).

Grading

<table>
<thead>
<tr>
<th>Component</th>
<th>Weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>Problem Sets</td>
<td>30%</td>
</tr>
<tr>
<td>Midterms (2)</td>
<td>40% (20% each)</td>
</tr>
<tr>
<td>Final Exam (Dec 14 Monday 9:45-11:45)</td>
<td>30%</td>
</tr>
</tbody>
</table>

There will be periodic problem sets. The problem sets will be mostly analytical but may also include some numerical problems. The latter type may involve the use of Excel or Matlab on the computer. I encourage you to work together on problem sets but each of you will hand in your own assignment. **Though you are encouraged to work in groups, you must acknowledge your collaborators in your solutions to the problem sets.**
Textbooks
There are two books that we will reference fairly extensively in the course:

Other references
Calculus and its applications to economics
*(Sundaram’s book is also highly recommended.)

Dynamic programming

Optimal control theory

Analysis

Numerical methods
Topics covered

1. Preliminaries
   Elements of set theory, logic, and proof
      *SB Appendix A1
      Sundaram Appendices A and B

   Properties of Euclidean space and metric space
   Sequence, convergence and limits, Cauchy sequence, vector space, norm, metric space, complete metric space, Banach space
      *SB Ch 10 and 12.1, 12.2
      *SLP Ch 3.1
      Sundaram, Ch 1.1 and 1.2
      Sundaram, Appendix C

   Topology of Euclidean spaces
   Open, closed, bounded, compact sets
      *SB Ch 12.3-12.6, Ch 29.

2. Multivariate calculus
   Functions: basic concepts
   Basic terminology of functions, continuity, monotonicity, partial and total derivatives, chain rule, higher order derivatives
      *SB Ch 13, 14.1-14.9
      Sundaram, Ch 1.4

   Functions: applications
   Intermediate and mean value theorems, Taylor’s Theorem, inverse and implicit function theorem
      *SB Ch 15, 30
      Sundaram, Ch 1.5 and 1.6

   Existence of solutions to optimization
   Weierstrass Theorem
      *SB Ch 30.1
      Sundaram, Ch 3

MIDTERM I

3. Static optimization
   Unconstrained optimization
   Quadratic forms, first order necessary conditions, second order sufficient conditions
Constrained optimization
Lagrangian method, first order necessary conditions, second order sufficient conditions, equality
and inequality constraints, Kuhn-Tucker Theorem, interpretation of Lagrangian multipliers,
envelope theorems, concave and quasiconcave functions, concave programming
Sundaram, Ch 5, 6, 7

Economic applications of static optimization
Utility maximization and expenditure minimization, Roy’s identity, Shephard’s lemma, Slutsky
matrix
*SB Ch 22

MIDTERM II

4. Dynamic optimization
Difference and differential equations
*Difference equation: SB 23.1, 23.2

Dynamic optimization: Calculus of variations, optimal control theory
The Calculus of Variations: Chiang Ch 2, 3, 6
The Hamiltonian Function: Chiang Ch. 7
More on Optimal Control: Chiang Ch 8
Infinite-Horizon Problems: Chiang Ch 5, 9
*Dorfman, R. (1969) An Economic Interpretation of Optimal Control Theory, American
Economic Review, 59(5) 817-831.
American Economic Review, 60(3) 518-522.
Appendices A.1 and A.3 of Barro and Sala-i-Martin (2003) Economic Growth, 3rd

5. Other possible topics
Maximum Theorem, Fixed Point Theorem, …

Disability Access
If you feel you need reasonable accommodations because of the impact of a disability, please: (1)
contact the KOKUA Program (V/T) at 956-7511 or 956-7612 in room 013 of the QLCSS (Queen
Lili’uokalani DCenter for Student Services); (2) speak with me privately to discuss your specific
needs. I will be happy to work with you and the KOKUA Program to meet access needs related
to a documented disability.